

SW-1.35a) $\Pr[\text{success to all } N \text{ receivers in one attempt}] = p^N$
 $\Pr[\text{unsuccessful to all } N \text{ receivers in one attempt}] = 1 - p^N$

$$\begin{aligned}\Pr[\text{success at } m=2] &= \Pr[\text{success at } m=2 \mid \text{not at } m=1] \Pr[\text{not at } m=1] \\ &\quad + \Pr[\text{success at } m=2 \mid \text{success at } m=1] \Pr[\text{success at } m=1] \\ &= p^N (1 - p^N) + 0 \cdot p^N \\ &= p^N (1 - p^N)\end{aligned}$$

generalizing...

$$\Pr[\text{success at } m] = p^N (1 - p^N)^{m-1}$$

$$\Pr[\text{success at } \leq m] = \sum_{n=1}^m p^N (1 - p^N)^{n-1}$$

-OR-

$$\begin{aligned}\Pr[\text{success at } \leq m] &= 1 - \Pr[\text{no success at } \leq m] \\ &= 1 - (1 - p^N)^m\end{aligned}$$

← these are equal →

b) For each receiver, success in exactly m intervals occurs with probability $p(1-p)^{m-1}$, which can be seen via

m	probability
1	p
2	$p(1-p)$
3	$p(1-p)^2$
\vdots	

Thus success in $\leq m$ intervals occurs with probability $\sum_{n=1}^m p(1-p)^{n-1}$
 For N independent receivers, this becomes

$$\left[\sum_{n=1}^m p(1-p)^{n-1} \right]^N$$

-OR-

$$\begin{aligned}\Pr[\text{success for a receiver in } \leq m \text{ intervals}] &= 1 - \Pr[\text{no success in } \leq m \text{ intervals}] \\ &= 1 - (1-p)^m\end{aligned}$$

For N independent receivers, this becomes

$$\left[1 - (1-p)^m \right]^N$$